

## PS 7 Physics 201 February 24, 2010 R.Shankar Due March 3.

1. In an LCR circuit we know the current has a maximum at  $\omega = \omega_0 = \sqrt{\frac{1}{LC}}$ . Show that the current falls to  $1/\sqrt{2}$  of the maximum if we go off  $\omega_0$  by  $\delta = R/2L$  provided  $\delta/\omega_0 \ll 1$ .
2. Find the impedance of the circuit with  $L$ ,  $C$  and  $R$  in parallel.
3. Consider a circuit element which is made of a  $C$  in parallel with an  $R + L$  in series as shown in Fig.1. Are there any  $\omega$ 's for which its impedance is real? If yes, at what  $\omega$ ?

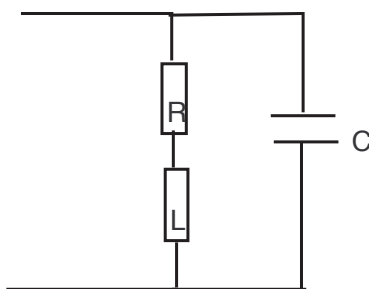


Figure 1: Can the impedance of this circuit be real? If so at what frequency?

4. You are given voltage source at  $\omega = 2000$  and a box that contains:  $R_1 = 100\Omega$ ,  $R_2 = 200\Omega$ ,  $C_1 = 1\mu F$ ,  $C_2 = 100\mu F$ , and  $L_1 = 1mH$ ,  $L_2 = 2mH$ . What will you pick if, using one resistor, one capacitor and one inductor in series you need to make a circuit with the smallest and largest  $|Z|$ ? Give the values of  $|Z|$  in both cases.
5. An AC source  $30 \cos 500t$  is connected to two impedances in series. The first is a resistor,  $Z_1 = 10\Omega$  and the second,  $Z_2$ , is made of a  $15\Omega$  resistor in series with a  $2\mu F$  capacitor. What is the power loss in across  $Z_2$ ?
6. I apply a voltage  $V(t) = 200 \cos 200\pi t$  to a capacitor with two concentric circular plates of radius  $4cm$  spaced  $2cm$  apart in the  $z$ -direction, with the upper plate positive at  $t = 0$ . Assuming the  $\mathbf{E}$  field is restricted to the plates, find the  $B$  field at a distance  $r$  from the center and half-way between the plates for all  $r$ . Evaluate its maximum amplitude in Tesla.