

II. (8)  $x^4 - 2 \leq x(1-x) - x^3$

$$x^4 - 2 \leq x - x^2 - x^3$$

$$x^4 + x^3 + x^2 - x - 2 \leq 0$$

$$\begin{array}{cccccc} 1 & 1 & 1 & -1 & -2 & \textcircled{1} \\ \downarrow & 1 & 2 & 3 & 2 & \\ 1 & 2 & 3 & 2 & 0 & \end{array}$$

$(x-1)(x^3 + 2x^2 + 3x + 2) \leq 0$

$$\begin{array}{cccccc} 1 & 2 & 3 & 2 & \textcircled{-1} \\ \downarrow & -1 & -1 & -2 & \\ 1 & 1 & 2 & 0 & \end{array}$$

$$(x-1)(x+1)(x^2+x+2) \leq 0$$

⊕

| x   | -1    | 1     |
|-----|-------|-------|
| x-1 | -     | - ⊕ + |
| x+1 | - ⊕ + | +     |
| ~   | +     | - +   |

$$x \in [-1, 1]$$

8. ⑥  $(x^3 - x)(-x^2 + x - 5) > 0$

$$x(x^2 - 1)(-x^2 + x - 5) > 0$$

⑥ ① ①

$$\Delta = 1 - 20 < 0$$

| x              | -1 | 0 | 1 |
|----------------|----|---|---|
| x              | -  | 0 | + |
| $x^2 - 1$      | +  | 0 | - |
| $-x^2 + x - 5$ | -  | - | - |
| $P(x)$         | +  | - | + |

$$x \in (-\infty, -1) \cup (0, 1)$$

7. ⑤  $(1-x) (x-2)^2 < 0$

①                  ②

| x         |   | 1 | 2 |
|-----------|---|---|---|
| $1-x$     | + | 0 | - |
| $(x-2)^2$ | + | + | 0 |
| $p(x)$    | + | - | - |

$$x \in (1, 2) \cup (2, +\infty)$$

⑥  $(x-2) (1-x)^3 \geq 0$

②                  ①

| x         |   | 1 | 2 |
|-----------|---|---|---|
| $x-2$     | - | - | 0 |
| $(1-x)^3$ | + | 0 | - |
| $p(x)$    | - | + | - |

$$x \in [1, 2]$$

# Ενότητα 19

7. β  $(-3x-2)(x-1)(5+2x) \leq 0$

$\left(-\frac{2}{3}\right) \quad \downarrow \quad \left(-\frac{5}{2}\right)$   
 $(1)$

| $x$     | $-\frac{5}{2}$ | $-\frac{2}{3}$ | 1     |
|---------|----------------|----------------|-------|
| $-3x-2$ | +              | + 0 -          | -     |
| $x-1$   | -              | -              | - 0 + |
| $5+2x$  | - 0 +          | +              | +     |
| $p(x)$  | +              | -              | +     |

$$x \in \left[-\frac{5}{2}, -\frac{2}{3}\right] \cup [1, +\infty).$$

# Εποραιο Μαθημα

---

Ερωτήματα 19

---

①  $\alpha \gamma \epsilon \zeta$

②  $\alpha$

③  $\alpha \beta \gamma$

④  $\alpha$

⑤  $\alpha \beta$

⑥  $\alpha$

⑦  $\alpha \gamma \epsilon$

⑧  $\alpha \gamma$

⑩  $\alpha \beta$

⑪  $\alpha \beta$ .